

# Near field phase mapping exploiting intrinsic oscillations of aperture NSOM probe

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**Abstract:** An innovative, simple, compact and low cost approach for phase mapping based on the intrinsic modulation of an aperture Near Field Scanning Optical Microscope probe is analyzed and experimentally demonstrated. Several nanoscale silicon waveguides are phase-mapped using this approach, and the different modes of propagation are obtained via Fourier analysis. The obtained measured results are in good agreement with the effective indexes of the modes calculated by electromagnetic simulations. Owing to its simplicity and effectiveness, the demonstrated system is a potential candidate for integration with current near field systems for the characterization of nanophotonic components and devices.

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**OCIS codes.** (120.5050) Phase measurement; (180.4243) Near-field microscopy; (130.2790) Guided waves .

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## 1. Introduction

The ability to measure light in the near field by a Near Field Scanning Optical Microscope (NSOM) plays an important role in high resolution imaging [1,2]. Nowadays, NSOM is widely used for the characterization of nano photonic structures, e.g. nano waveguides [3,4], photonic crystals [5], plasmonic structures [6,7] and metamaterials [8].

Typically an NSOM measures the intensity of the light and does not reveal the complex nature of the measured electromagnetic field. In order to measure both the phase and the amplitude of the field, various systems have been proposed and demonstrated both in aperture and in apertureless configurations. For example, in an Aperture Heterodyne NSOM the light is collected by the probe and combined with a reference arm to allow simultaneous measurement of the amplitude and the phase of the light [9-11]. This technique uses Acousto Optic Modulators (AOMs) in order to shift the frequency of the reference arm with respect to the collecting arm and was used for the characterization of large variety of nano-photonic devices [12-17]. These AOMs are integrated into an interferometer that consists of an existing NSOM apparatus. In other works [18,19], the phase and amplitude measurement has been obtained by introducing an additional phase modulator into one of the arms of the interferometer, a modulation that introduces several spectral components in the reference arm which in turn interfere with the probe arm.

In order to maintain constant distance from the device under test (DUT) and to improve the signal whilst measuring fragile samples having abrupt topographical variations one can use the NSOM scanning in tapping mode, in which the NSOM probe is oscillating with respect to the sample. This mode of operation is often exploited in Apertureless NSOMs [20] (ANSOM), where the light scattered from a metallic tip is collected in the far field and is demodulated at one of the harmonics of the tip's oscillating frequency in order to eliminate background scattering [21]. Such ANSOMs have been combined with heterodyne systems where, various combinations of the probes frequency and AOM frequency have been used in order to extract both the phase and the amplitude of the signal [22-25].

In this paper, we exploit the intrinsic modulation of the NSOM tip operating in tapping mode to measure the phase of the signal in the near field using an aperture NSOM. The

system is based on an all-fiber interferometer. We show this intrinsic modulation introduces several spectral components that interfere with the reference arm and introduce a signal that contains information representing the phase and the amplitude of the signal. The method is compact, cost effective, align-free, shot-noise limited and does not require external modulators. The system can be integrated to an existing NSOM setup in relative ease and has high potential as a characterization tool of various nanophotonic structures. The benefits of the system are demonstrated through the near field characterization of several silicon nanophotonic devices, including straight and serpentine like ridge waveguides as well as the recently demonstrated local oxidation of silicon (LOCOS) waveguides [26]. To the best of our knowledge, near field phase measurements of LOCOS waveguides are demonstrated here for the first time.

The paper is structured as follows: Section 2 outlines the concept of operation and describes the experimental setup. In section 3 we demonstrate the experimental results obtained with the system. Section 4 concludes the paper.

## 2. Concept of operation and experimental arrangement

The experimental setup is illustrated schematically in Fig. (1). A 1550 nm wavelength TE (in plane) polarized light emitted from a diode laser is split by a 90/10 polarization maintaining (PM) fiber beam splitter (BS) where the majority of light is sent via a PM lensed fiber into a silicon waveguides (WG) serving as the DUT. Metal coated NSOM probes (With an apex varying between 250 and 300 nm. This aperture size determines roughly the resolution of our system) are brought into proximity with the DUT and kept in contact with its surface using the tapping feedback mechanism in a commercial NSOM system (Nanonics MultiView 4000). The light is collected by the NSOM tip, combined with the reference arm using a 50/50 PM BS and detected by an InGaAs Photo Detector (PD, Thorlabs DET01CFC). The NSOM probe is modulated at a frequency  $f_{\text{probe}}$  around 40 KHz, which is the characteristic eigen-frequency of the tuning fork of the tip. Such a relatively low frequency component can be detected and demodulated with relative ease with a standard detector and Lock In Amplifier (LIA, SR-830) either in quadrature (Y) or in phase (X) modes.

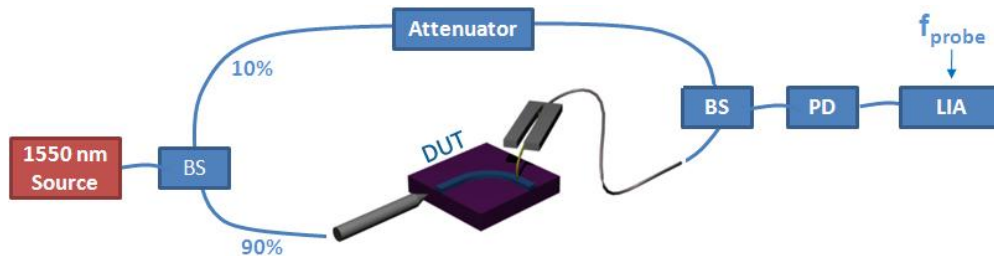


Fig. 1. Experimental arrangement of the NSOM probe modulated interferometer. (BS – Beam Splitter, DUT – Device Under Test, PD – Photo Detector, LIA – Lock In Amplifier)

As in any interferometer, special attention is needed in order to avoid phase drifts due to temperature, and/or mechanical instabilities. This is achieved by: 1- setting the optical paths of the interferometer arms to equal lengths in order to be immune to thermo-mechanical and frequency drifts, and 2- by thermal and mechanical insulation of the system using a “Minus-K” bench top vibration isolation platform and a “home made” acoustic hood. The former has the additional benefit of protecting the probe from getting damaged.

In order to evaluate the signal derived from the LIA at the tip's frequency, we assume that the mechanical modulation of the probe is converted to an amplitude modulation of the probed light while interacting with the evanescent field propagating along the WG. A schematic graphic representation of the process is illustrated in Fig. 2, where the tuning fork attached to the NSOM probe is illustrated in contact with the WG. We assume that the

electric field coupled to the probe is proportional to the evanescent field of the WG mode having a decaying characteristic length of  $d$ , and amplitude  $E_0$  at the surface of the WG. A graphical representation of this evanescent field is illustrated in the white figure in Fig. 2. We work in tapping mode, with the tip oscillating at the eigen-frequency of the tuning fork and tip assembly ( $\omega_{probe}$ ) and an oscillation amplitude of  $h$ . Therefore, the tip position can be described as  $z = z_0 + h \cos(\omega_{probe}t)$ , whilst  $z_0$  is the mean position of the probe, as illustrated in Fig. 2. The red sine wave illustrated in Fig. 2 demonstrates the resultant modulated field with a frequency (to first order in  $h/d$ ) of  $\omega_{probe}$  and amplitude corresponding to the two points  $z_1$  and  $z_2$  illustrated in the figure.

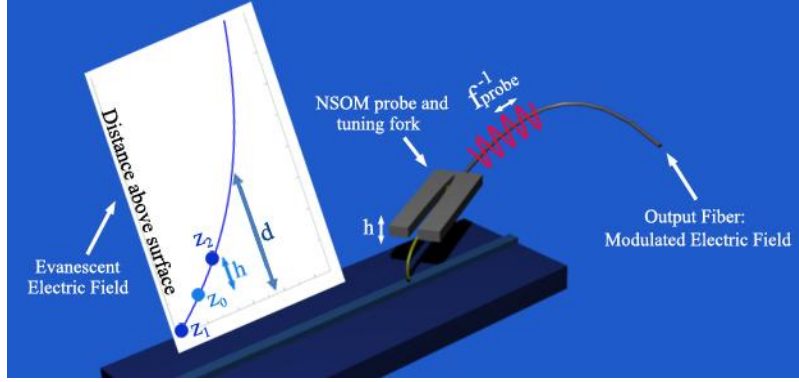


Fig. 2. Schematic illustration of the conversion of mechanical modulation into amplitude modulation of the probed electric field: The NSOM probe oscillates due to modulation of the tuning fork and probes the evanescent decaying field, resulting in a modulated electric field.

The intensity, at the photo-detector is proportional to the absolute squared value of this signal arm, summed with a reference arm having an amplitude  $b$  and a constant phase  $\phi_0$ , yielding the following expression:

$$\bar{V}(x, y, t) = \left| a \exp\left(-\frac{h}{d} \cos(\omega_{probe}t)\right) \exp(i\phi(x, y) - i\omega t) + b \exp(-i\omega t + i\phi_0) \right|^2 \quad (1)$$

Where we defined  $a$  as the amplitude of the probed field at  $z_0$ ,  $\omega$  as the carrier frequency and  $\phi(x, y)$  as the phase accumulated on the plane of the device by the probe arm. We assume negligible background fields due to the use of aperture probes in our system. In the case of apertureless probes the background scattering should be taken into account in the same manner as has been analyzed in ref [23,25]. Equation (1), expanded to modified Bessel functions of the first kind, to first order in  $a$  can be written for the Fourier component of  $\omega_{probe}$  as:

$$V(x, y, t) = 4abI_1\left(\frac{h}{d}\right) \cos(\phi(x, y)) \cos(\omega_{probe}t) \approx 2ab \frac{h}{d} \cos(\phi(x, y)) \cos(\omega_{probe}t) \quad (2)$$

Where  $I_1$  is the first modified Bessel function of the first kind,  $\Delta\phi(x, y)$  is defined as  $\phi(x, y) - \phi_0$  and the approximation holds for  $h/d \ll 1$ . This later assumption is reasonable because typical values of  $h$  are  $\sim 20$  nm, whereas  $d$  is typically at least order of magnitude larger. In the case where we have single mode propagation, Eq. (2) implies that by measuring this Fourier component one obtains a direct measurement of the electric field, and thus the wave vector's magnitude and direction can be found. Moreover, enhancement of the signal to noise ratio is obtained similarly to a conventional Heterodyne, and thus increasing the

intensity in the reference arm can lead to a shot noise limited detection system, as reported in ref [10]. We shall refer to this demodulated signal as the Phase NSOM (PNSOM) signal. In the case where the probed electric field consists of several k-vectors (multi mode propagation), the Fourier component will be a superposition of terms such as in Eq. (2) in the following manner:

$$V(r, t) = 2b \sum_n a_n \frac{h}{d_n} \cos(\Delta\phi_n) \cos(\omega_{probe} t) \quad (3)$$

As before, the effective indices of refraction can be derived by Fourier analysis of the signal. However, in this case, caution should be taken in the interpretation of the amplitudes of the different propagation modes, due to the possible differences between the evanescent lengths  $d_n$ . These differences can be compensated in the Fourier analysis if we assume all the interactions to be pure evanescent, and use the conservation of momentum:  $k_0^2 = k_0^2 n_{eff}^2 - d^{-2}$ . In addition, due to the signal being inverse proportional to the decaying length  $d$ , delocalized modes that have decaying lengths much larger than the oscillation amplitude  $h$  might suffer a degradation in signal to noise ratio due to the small value of the modulation depth  $h/d$ . However, this may be compensated by the amplification of the heterodyne approach.

### 3. Experimental results

To demonstrate the concept described above, we first characterize a silicon WG with cross sectional dimensions of 450 nm width and 240 nm height. A cross section scanning electron micrograph (SEM) of the WG is presented in Fig. 3a. The measured superimposed PNSOM signal and topography, and the PNSOM signal for 1550 nm excitation wavelength are shown in Fig. 3b and 3c respectively.

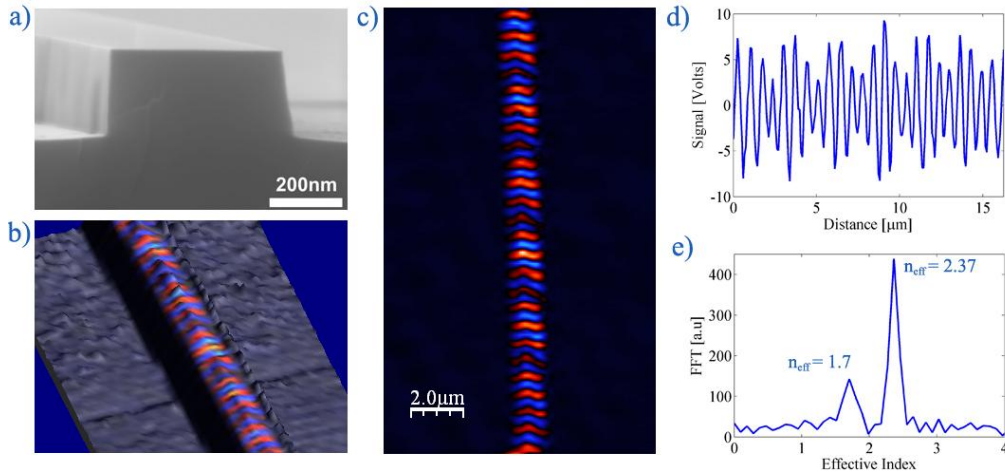


Fig. 3. (a) cross section SEM of the WG (b) Superimposed PNSOM signal and topography (c) Raw PNSOM Signal (d) Cross section of the amplitude-phase signal in the direction of propagation of light (e) FFT Spectrum of the cross section, displayed in Effective index units.

Figure 3d shows a cross section of the phase image (Fig. 3c), whereas Fig. 3e shows the spatial spectrum of the signal along the propagation direction, obtained by a Fast Fourier Transform (FFT) of the cross section in Fig. 3d. The result clearly indicates a dominant mode with effective index of  $2.37 \pm 0.1$  (the error was estimated from the width of the peak in the spectral domain). Additionally, there is another peak with smaller amplitude and an effective index of  $1.70 \pm 0.1$ . These experimental values are in excellent agreement with the numerical electromagnetic simulation results (obtained with COMSOL MultiPhysics), which correspond to a TM-like mode with refractive index of 1.68 and a TE-like mode with index of

refraction of 2.33. The existence of the TM mode in our WG can be explained by the TE/TM conversion in the waveguide as a result of fabrication imperfections and a bent section in the WG. This bend is needed for PNSOM measurements as it allows spatial separation between the guided modes and the radiation modes emanating from the coupling region between the lensed fiber and the WG. We note that concluding the actual amplitude ratio between these two modes of the amplitude from the FFT figure might be misleading. These measured amplitudes can differ from the real amplitudes due to two reasons. The first, mentioned before and illustrated by Eq. (3), is the fact that our PNSOM signal is linear with the inverse of the evanescent length, and thus each mode has a different evanescent length yielding different amplitudes in the FFT. The second is due to the vectorial transfer function of the NSOM tip, which is anticipated to be stronger for the TE-like mode [27].

Next, we demonstrate the phase characterization in the case of LOCOS WGs. The WGs are identical to those reported in [26], with cross sectional dimensions of 450nm width on the top, and 250nm height. The WG consists of a silicon core with silica cladding both on its side walls and on its bottom, as is illustrated in Fig. 4a where the cross section SEM image of the LOCOS WG is presented. Based on the dimensions obtained by the SEM image, we performed a finite-element eigen-mode simulation (COMSOL). The fundamental field distribution of the fundamental WG mode is superimposed upon the SEM image in Fig. 4a. This fundamental TE-like mode has an effective index of 2.54. From these simulations we found that a second TM-like mode is also supported by the structure, with an effective index of 1.85. Figure 4d shows a cross section of the phase image (Fig. 4c), whereas Fig. 4e shows the spatial spectrum of the signal along the propagation direction, obtained by a Fast Fourier Transform (FFT) of the cross section in Fig. 4d.

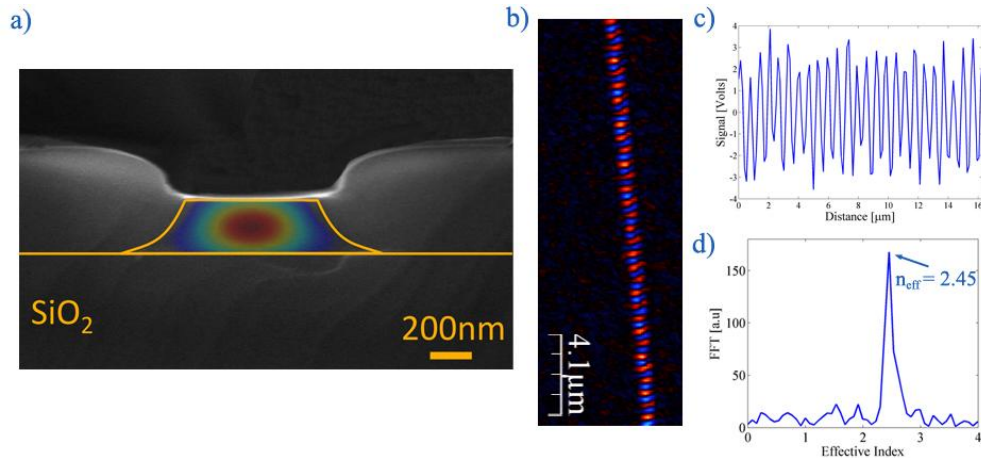


Fig. 4. (a) SEM of LOCOS WG with superimposed simulated profile of the fundamental guided mode (b) LOCOS WG PNSOM signal (c) LOCOS WG PNSOM signal cross section in the propagation direction (d) FFT Spectrum of the cross section, displayed in Effective index units.

A distinct Fourier component corresponding to the value of effective index of  $2.45 \pm 0.1$  is obtained. This value is very close to the simulated value of 2.54 reported in [26]. In addition, two minor Fourier components can be seen in the Fig. 4b. These two components correspond to the effective indexes of silica, and the second TM-like mode mentioned earlier.

Finally, in order to demonstrate the characterization of a more complex in-plane light propagation we characterize silicon WG that is bent in s-shape serpentine manner. Figure 5a shows a SEM image of the device whereas Fig. 5b presents the topography and superimposed PNSOM signal. It is clear that the phase signal follows the topography of the WG. This can be shown more clearly in Fig. 5c where one can see the elaborate phase distribution of the

light propagating through the device. Clear slanted phase fronts that follow the topography of the WG are shown. In addition, one can identify phase fronts with a longer wave-length that do not follow that WG. These phase fronts are most likely radiation and scattering modes that originate from sidewall roughness and from the bending of the WG. In Fig. 5d the electric field obtained via a finite difference time domain (FDTD) simulation of this s-shaped WG are presented. The simulation results contain the same features that were observed in the measurements, including both the guided and the radiation modes (the radiation modes part in the image has been amplified in order to improve their visibility).

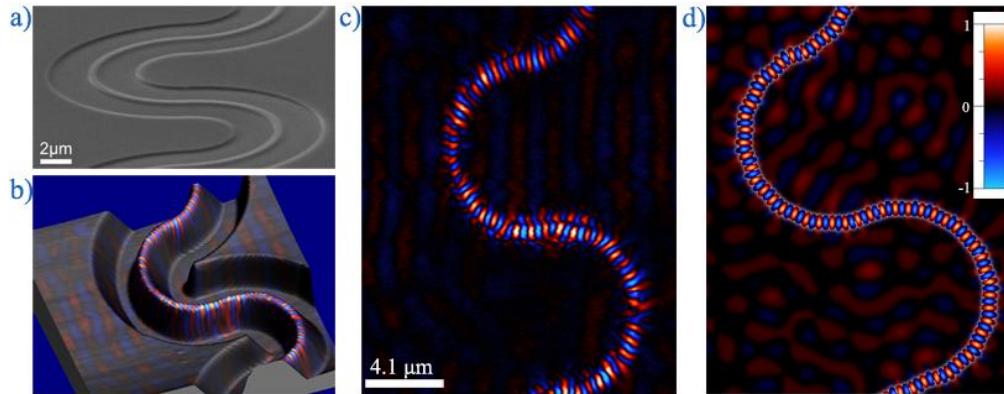


Fig. 5. (a) SEM image of Si serpentine WG (b) Superimposed PNSOM signal on AFM topography (c) PNSOM raw signal (d) FDTD simulation of the s-shaped WG field distribution, in order to improve the visibility the background of the image is amplified.

#### 4. Summary

An innovative method which exploits the intrinsic amplitude modulation of an aperture NSOM probe in tapping mode is experimentally demonstrated and used for the characterization of several sub-micron silicon light guiding devices. We measured the phase profile in these different WGs and used these measurements to perform a modal analysis that was found to be in good agreement with computer simulations. The demonstrated method is compact, cost effective, align-free, and shot-noise limited. Such a system can be integrated to an existing NSOM setup, in relative ease and is thus a potential candidate for the characterization tool of various nanophotonic structures.

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